



# A multi-level TCP model with heterogeneous RTTs

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## Motivation

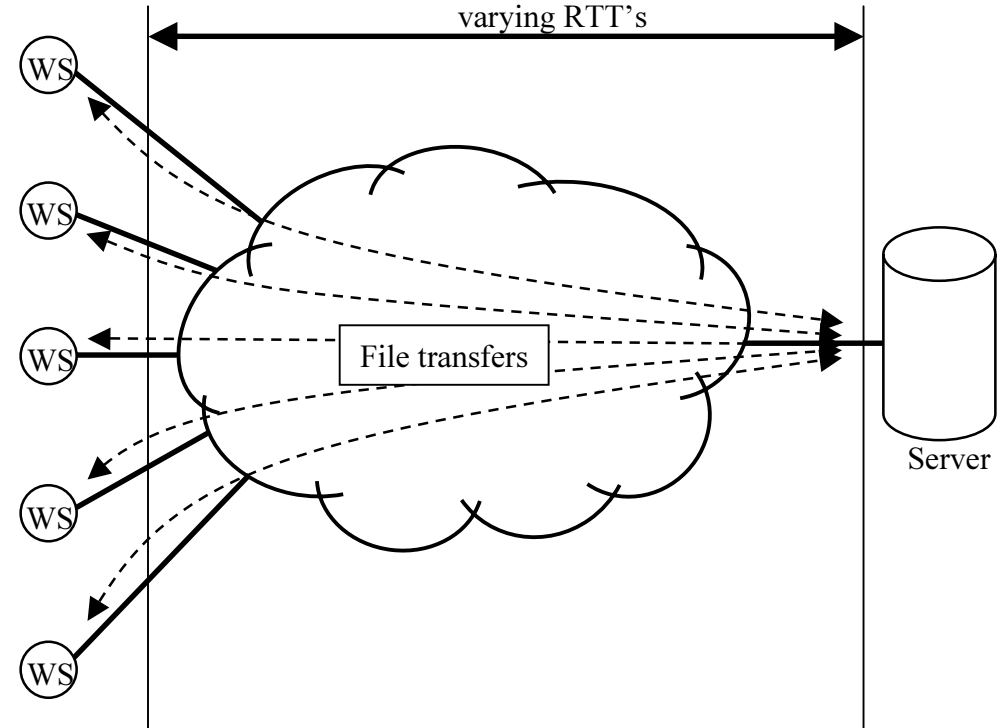
- Most Internet traffic carried by TCP
- Main performance measures: throughput and delay

## Scenario

- Requests arrive randomly, files have random lengths
- Issues: packet losses, RTTs
- Bottleneck(s): access link, network, server link

## Purpose

- Understand how above affects delay performance
- Quantify the dependencies





## Earlier work

- Paper presented at ITC-18 (Berlin, August 31 - September 5, 2003)
  
- Simplified scenario
  - captures sending rate limitation, one bottleneck link (losses), ...
  - ... but can account for only one RTT!
  
- Main interest: mean delay
  - Slow start compensation heuristic expressed in a way that requires file lengths to be long enough that TCP steady state is reached
  - $\Rightarrow$  Model for relatively long file transfers (depending on the bandwidth delay product)
  
- Results promising, but applicability limited



## Present study

- We only consider averages (mean values)
- Main objective: relax assumption of a single RTT
  - Flows with different RTTs share the capacity such that the flows with smaller RTT get more throughput than flows with larger RTTs
  - Assumption: flows are grouped into classes according to RTT
- Include effect of access rate limitation
- Express initial slow start effect such that files of any size can be handled
  - Short files (web mice) simply never leave slow start and will never reach TCP “steady state”



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## Other approaches

- Fayolle [1980] model: DPS (Discriminatory Processor Sharing), idealized model where flows share the capacity in a weighted manner
  - does not include effect of rate limitations
  - Bu & Towsley [2001] have used the Fayolle model to consider different RTTs
  
- Ayesta et al. [2003] have considered the conditional mean delay (given the file size) of short flows (web mice)
  - do not explicitly take into account rate limitations, but study the effect of rate limitations on accuracy of Poisson arrival assumption at the buffer (and packet loss estimates)
  - basically only use their model in load scenarios where bottleneck sharing does not occur
  
- Extending the earlier GPS model difficult
  - Possible to make assumptions under which everything is Markovian
  - Can be generalized to multiple classes and one can (in theory) construct the generator of the multidimensional process
  - Computationally too intensive for any realistic system



## Modeling approach: step 1

- Consider a single link and one RTT
- Assume files lengths exponentially distributed with mean  $1/\mu$
- Model the time evolution of the mean number of flows in the system,  $N(t)$ , and the mean sending rate of the TCP aggregate,  $\lambda(t)$

$$\begin{cases} \frac{dN(t)}{dt} = \nu - \mu \overbrace{\lambda(t)(1-P(t))}^{C(t)} (1 - \pi_0(t)) \\ \frac{d\lambda(t)}{dt} = (1 - P(t)) \frac{N(t)}{R^2} - P(t) \frac{\lambda^2(t)}{2N(t)} \end{cases}$$

- Idea: use the ideal PS model, but with a reduced goodput,  $C(t)$ ; goodput reduction determined by TCP's dependence on RTT and packet loss
- $\pi_0(t)$  given by a quasi-stationarity approximation of the corresponding PS system
- $P(t)$  given by the packet loss probability in an M/G/1/K queue with arrival rate  $\lambda(t)$



## Modeling approach: step 2

- Model for single link case with  $M$  classes each with own RTT
- Assume that all classes have a common mean file length  $1/\mu$
- With Poisson flow arrivals, the total number of flows in the system still behaves as in a PS system for any work conserving service discipline
  - Mean number of flows in each class is divided in proportion to the goodput share of each class
  - Goodput of the system,  $C(t)$ , takes into account the sending rate obtained by each TCP class (captures different RTTs)
  - Classes share the bottleneck bandwidth such that link is full

$$\begin{cases} \frac{dN(t)}{dt} = \sum_i v_i - \mu \overbrace{\sum_i \lambda_i(t)(1-P(t))}^{C(t)} (1 - \pi_0(t)) \\ \frac{d\lambda_i(t)}{dt} = (1-P(t)) \frac{N_i(t)}{R_i^2} - P(t) \frac{\lambda_i^2(t)}{2N_i(t)}, i = 1, \dots, M \end{cases}$$
$$N_i(t) = \frac{v_i / \lambda_i(t)}{\sum_i v_i / \lambda_i(t)} N(t)$$



## Modeling approach: step 3

- Effect of rate limitation
  - Observation: Each flow is only limited by its sending rate as long as number of ongoing flows is less than it takes to fill the bottle neck link  $\Rightarrow$  M/G/ $\infty$  model. When this point is exceeded the system switches to processor sharing mode.
  - Which operating region is reached is determined by comparing the PS system sending rate estimate to the actual sending rate limit

$$r_i = \min(\lambda_i^{\max}, \lambda_i(1 - P) / N)$$

- Mean delay,  $D_j$ , consists of
  - length of slow start (time it takes to reach estimated sending rate) +
  - time to send remaining file at the estimated sending rate
- Mean number of flows:
  - If  $r_i$  determined by the PS limit, then mean number of flows equals  $N$
  - If  $r_i$  determined by sending rate limit, then mean number of flows in an M/G/ $\infty$  model with arrival rate  $n_i$  and mean service time  $D_j$





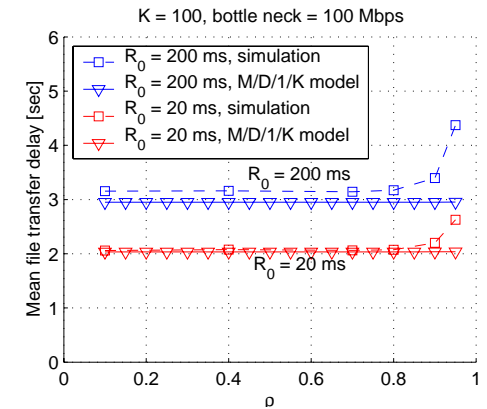
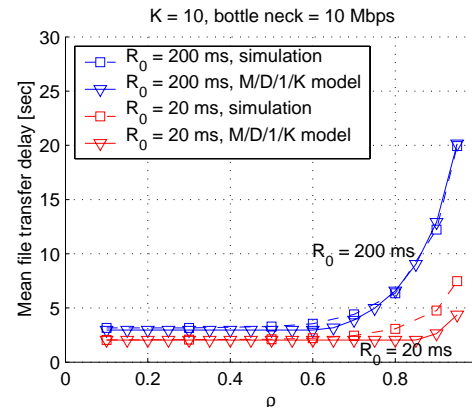
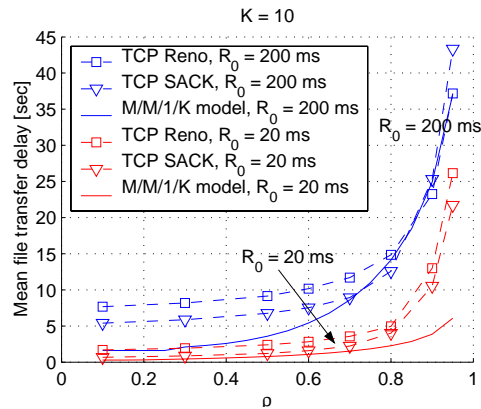
## Validation

- Validation concerns only the steady state results (no dynamics)
- Tests with:
  - different TCP versions (Reno, Sack)
  - access speed / bottle neck speed ratios
  - different buffer sizes
  - different RTTs
  - different file size distributions
  - different queuing models (M/M/1/K, M/D/1/K)
  
- Results on
  - mean number of customers
  - mean delays

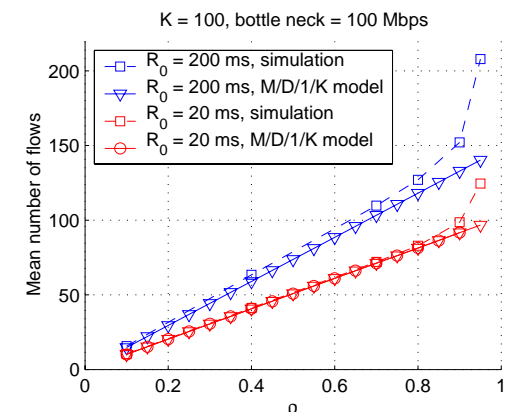
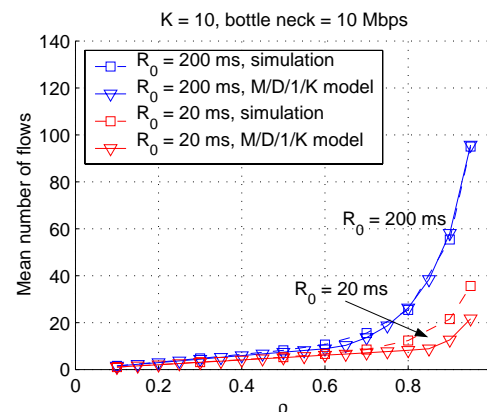
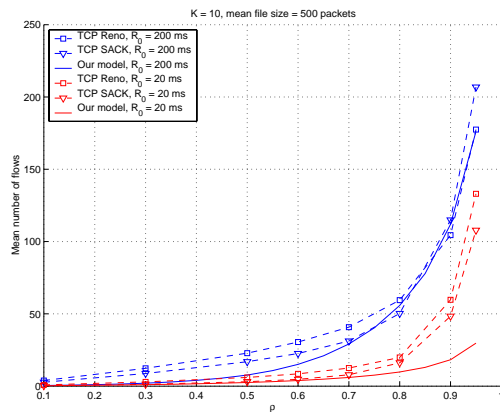


# Single RTT tests: effect of access rate limitation

## Mean delays

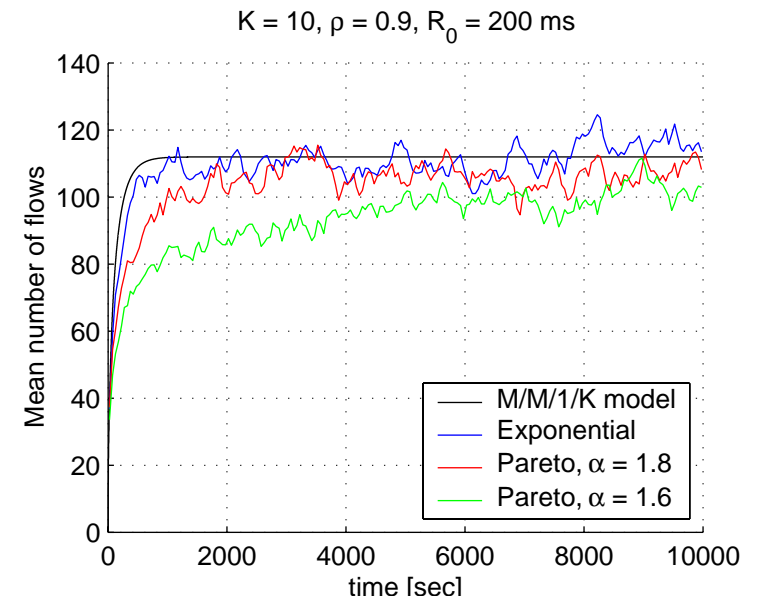
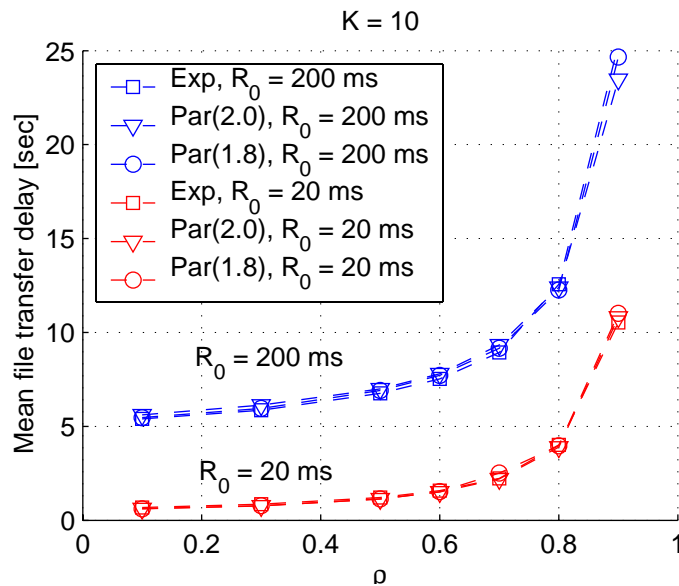


## Mean number of flows



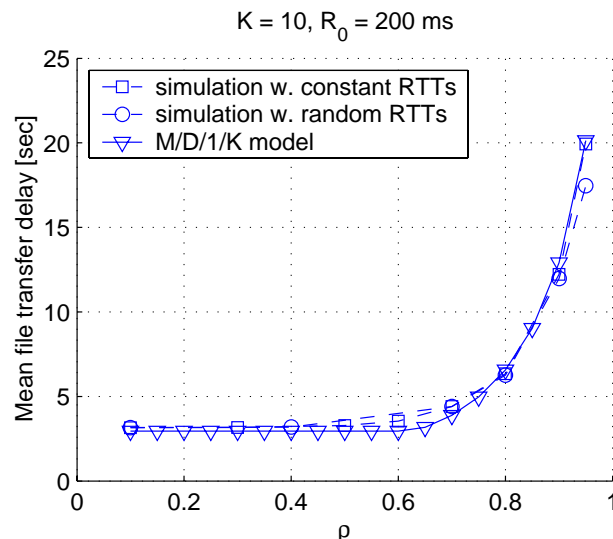
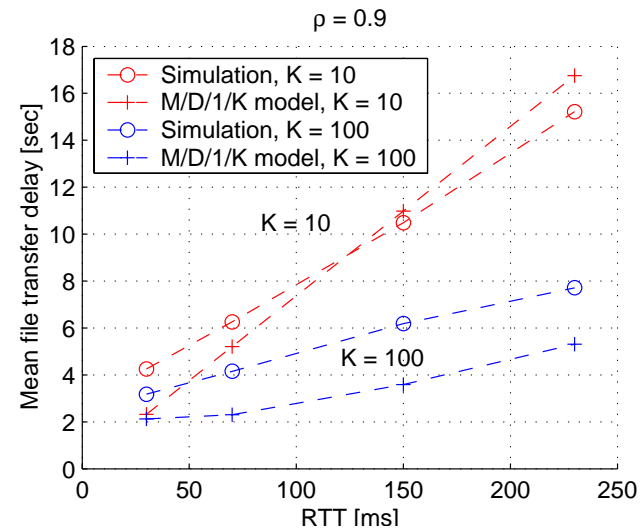
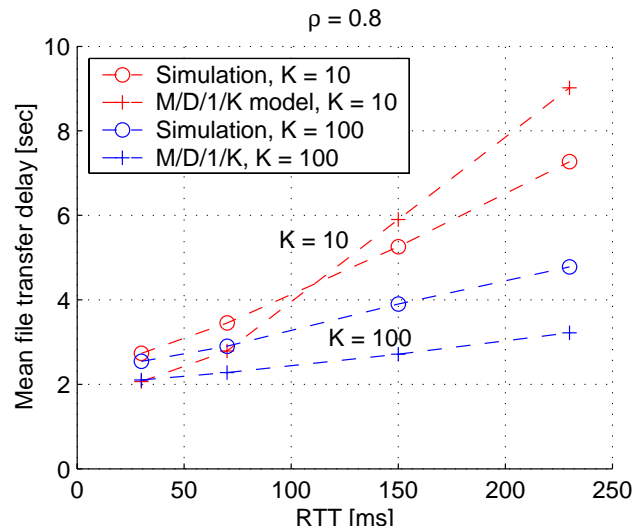


# Single RTT tests: insensitivity and dynamics





# Multiple RTT classes and random RTTs



- RTTs  $\sim U(10, 390)$  ms
- drawn independently for each file transfer
- mean delay still almost the same as with constant RTT of 200 ms



## Conclusions

- Model for mean delays of TCP sources sharing a single bottleneck
  - Captures unequal sharing due to different RTT classes,
  - Effect of access rate limitation, and
  - Initial slow starts
  
- Results are qualitatively correct but accuracy depends on parameters
  - Typically more accurate as the ratio of access bandwidth to the bottleneck bandwidth decreases ( $\Rightarrow$  more multiplexing of TCP sources)
  
- Open issues
  - Effect of retransmission timeouts, especially during slow start
    - We assume that TCP operates perfectly according to AIMD without time outs
  - Packet loss model (M/D/1/K) not very accurate
    - Packet arrival process is actually more like a batch arrival process (instead of Poisson)